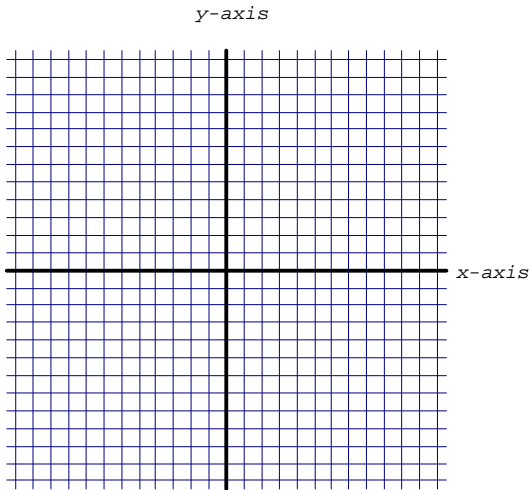


1. Verify that  $f(x) = \sqrt{x-4}$  where  $x \geq 4$  and  $g(x) = x^2 + 4$  where  $x \geq 0$  are inverse functions by:
- Using  $f[g(x)]$  and  $g[f(x)]$
  - Graphing



- Using  $f'(x)$  and  $g'(x)$ .
2. Which of the functions is not one-to-one?
- $f(x) = \cos x$ ,  $0 \leq x \leq \pi$
  - $f(x) = \sin x$ ,  $0 \leq x \leq \pi$
  - $f(x) = x^3$
3. Find the inverse of  $f(x) = \sqrt[3]{5x-2}$ .
4.  $f(x)$  is a one-to-one function with the following properties:
- Domain:  $x \geq 2$
  - Range:  $y \geq 0$
  - Passes through (5,8).
- If the inverse of  $f(x)$  is  $g(x)$ , find:

Domain of  $g(x)$  \_\_\_\_\_ Range of  $g(x)$  \_\_\_\_\_

A point on the graph of  $g(x)$  \_\_\_\_\_

5. Simplify:  $\ln \frac{\sqrt[3]{x}}{y^2}$  \_\_\_\_\_

6. Find to four decimal places.  $\ln 0.83$  \_\_\_\_\_

7. Solve for  $x$  to four decimal places.

a)  $\ln 8x - 3 \ln x^2 = \ln 4$

b)  $4e^{5x} = 23$

8. Find  $\frac{dy}{dx}$ .

a)  $y = x \ln x - x$

b)  $y = (\ln x)^3$

c)  $y = \text{Arc cos } 2x$

d)  $y = 2 \text{Arc tan } \sqrt{x}$

e)  $y = e^{5-2x}$

f)  $y = \log_{10} x^2$

g)  $y = e^{2x} \sin 5x$

h)  $y = x^3 \ln(2x)$

9. Find  $\frac{dy}{dx}$  using implicit differentiation.

$$x^3 + \text{Arc tan } y = e^{5x}$$

10. Use logarithmic differentiation to find  $\frac{dy}{dx}$ .

$$y = \sqrt[3]{\frac{x+1}{x-1}}$$

11. Find:

a)  $\text{Arc cos} \left( -\frac{1}{2} \right)$

b)  $\text{Arc sin} \left( \sin \frac{p}{9} \right)$

c)  $\sin \left( \text{Arc cos} -\frac{12}{13} \right)$

12. Find the limits:

a)  $\lim_{x \rightarrow \frac{p}{2}} \frac{1 - \sin x}{1 + \cos 2x}$

b)  $\lim_{x \rightarrow \infty} \frac{5x^2 - 3x}{7x^2 + 1}$

c)  $\lim_{x \rightarrow \infty} \frac{x^2 + e^x}{x + e^x}$

d)  $\lim_{x \rightarrow \infty} \left( 1 + \frac{3}{x} \right)^{2x}$

Hint: Let  $y = \left( 1 + \frac{3}{x} \right)^{2x}$

